



JERRY M. STRAKA

# Cloud and Precipitation Microphysics

Principles and Parameterizations

CAMBRIDGE

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Principles and Parameterizations

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# Contents

<i>Preface</i>	<i>page</i> xiii
<b>1 Introduction</b>	<b>1</b>
1.1 Cloud and precipitation physics and parameterization perspective	1
1.2 Types of microphysical parameterization models	2
1.3 Warm-rain parameterizations	4
1.4 Cold-rain and ice-phase parameterizations	5
1.5 Hydrometeor characteristics overview	7
1.6 Summary	17
<b>2 Foundations of microphysical parameterizations</b>	<b>19</b>
2.1 Introduction	19
2.2 Background	19
2.3 Power laws	21
2.4 Spectral density functions	23
2.5 Gamma distributions	27
2.6 Log-normal distribution	42
2.7 Microphysical prognostic equations	51
2.8 Bin microphysical parameterization spectra and moments	57
<b>3 Cloud-droplet and cloud-ice crystal nucleation</b>	<b>59</b>
3.1 Introduction	59
3.2 Heterogeneous nucleation of liquid-water droplets for bulk model parameterizations	61
3.3 Heterogeneous liquid-water drop nucleation for bin model parameterizations	68
3.4 Homogeneous ice-crystal nucleation parameterizations	70
3.5 Heterogeneous ice-crystal nucleation parameterizations	72

<b>4 Saturation adjustment</b>	<b>78</b>
4.1 Introduction	78
4.2 Liquid bulk saturation adjustments schemes	81
4.3 Ice and mixed-phase bulk saturation adjustments schemes	86
4.4 A saturation adjustment used in bin microphysical parameterizations	91
4.5 Bulk model parameterization of condensation from a bin model with explicit condensation	93
4.6 The saturation ratio prognostic equation	97
<b>5 Vapor diffusion growth of liquid-water drops</b>	<b>101</b>
5.1 Introduction	101
5.2 Mass flux of water vapor during diffusional growth of liquid-water drops	102
5.3 Heat flux during vapor diffusional growth of liquid water	106
5.4 Plane, pure, liquid-water surfaces	109
5.5 Ventilation effects	116
5.6 Curvature effects on vapor diffusion and Kelvin's law	118
5.7 Solute effects on vapor diffusion and Raoult's law	120
5.8 Combined curvature and solute effects and the Kohler curves	121
5.9 Kinetic effects	122
5.10 Higher-order approximations to the mass tendency equation	124
5.11 Parameterizations	129
5.12 Bin model methods to vapor-diffusion mass gain and loss	134
5.13 Perspective	138
<b>6 Vapor diffusion growth of ice-water crystals and particles</b>	<b>139</b>
6.1 Introduction	139
6.2 Mass flux of water vapor during diffusional growth of ice water	140
6.3 Heat flux during vapor diffusional growth of ice water	141
6.4 Plane, pure, ice-water surfaces	141
6.5 Ventilation effects for larger ice spheres	142
6.6 Parameterizations	143
6.7 Effect of shape on ice-particle growth	148
<b>7 Collection growth</b>	<b>152</b>
7.1 Introduction	152
7.2 Various forms of the collection equation	153
7.3 Analysis of continuous, quasi-stochastic, and pure-stochastic growth models	155

7.4	Terminal velocity	164
7.5	Geometric sweep-out area and gravitational sweep-out volume per unit time	165
7.6	Approximate polynomials to the gravitational collection kernel	165
7.7	The continuous collection growth equation as a two-body problem	166
7.8	The basic form of an approximate stochastic collection equation	168
7.9	Quasi-stochastic growth interpreted by Berry and Reinhardt	169
7.10	Continuous collection growth equation parameterizations	173
7.11	Gamma distributions for the general collection equations	177
7.12	Log-normal general collection equations	183
7.13	Approximations for terminal-velocity differences	188
7.14	Long's kernel for rain collection cloud	191
7.15	Analytical solution to the collection equation	194
7.16	Long's kernel self-collection for rain and cloud	195
7.17	Analytical self-collection solution for hydrometeors	196
7.18	Reflectivity change for the gamma distribution owing to collection	197
7.19	Numerical solutions to the quasi-stochastic collection equation	198
7.20	Collection, collision, and coalescence efficiencies	222
<b>8</b>	<b>Drop breakup</b>	<b>231</b>
8.1	Introduction	231
8.2	Collision breakup of drops	232
8.3	Parameterization of drop breakup	234
<b>9</b>	<b>Autoconversions and conversions</b>	<b>253</b>
9.1	Introduction	253
9.2	Autoconversion schemes for cloud droplets to drizzle and raindrops	255
9.3	Self-collection of drizzle drops and conversion of drizzle into raindrops	264
9.4	Conversion of ice crystals into snow crystals and snow aggregates	264
9.5	Conversion of ice crystals and snow aggregates into graupel by riming	267
9.6	Conversion of graupel and frozen drops into small hail	270

9.7	Conversion of three graupel species and frozen drops amongst each other owing to changes in density by collection of liquid particles	271
9.8	Heat budgets used to determine conversions	272
9.9	Probabilistic (immersion) freezing	278
9.10	Immersion freezing	283
9.11	Two- and three-body conversions	283
9.12	Graupel density parameterizations and density prediction	289
9.13	Density changes in graupel and frozen drops collecting cloud water	290
9.14	Density changes in graupel and frozen drops collecting drizzle or rain water	290
9.15	More recent approaches to conversion of ice	291
<b>10</b>	<b>Hail growth</b>	<b>293</b>
10.1	Introduction	293
10.2	Wet and spongy hail growth	297
10.3	Heat-budget equation	298
10.4	Temperature equations for hailstones	301
10.5	Temperature equation for hailstones with heat storage	302
10.6	Schumann–Ludlam limit for wet growth	304
10.7	Collection efficiency of water drops for hail	306
10.8	Hail microphysical recycling and low-density riming	307
<b>11</b>	<b>Melting of ice</b>	<b>312</b>
11.1	Introduction	312
11.2	Snowflakes and snow aggregates	313
11.3	Graupels and hailstones	313
11.4	Melting of graupel and hail	315
11.5	Soaking and liquid water on ice surfaces	326
11.6	Shedding drops from melting hail or hail in wet growth	328
11.7	Parameterization of shedding by hail particles of 9–19 mm	330
11.8	Sensitivity tests with a hail melting model	333
<b>12</b>	<b>Microphysical parameterization problems and solutions</b>	<b>336</b>
12.1	Autoconversion of cloud to drizzle or rain development	336
12.2	Gravitational sedimentation	338
12.3	Collection and conversions	340
12.4	Nucleation	343
12.5	Evaporation	344

12.6 Conversion of graupel and frozen drops to hail	344
12.7 Shape parameter diagnosis from precipitation equations	345
<b>13 Model dynamics and finite differences</b>	<b>346</b>
13.1 One-and-a-half-dimensional cloud model	346
13.2 Two-dimensional dynamical models	348
13.3 Three-dimensional dynamical model	355
<i>Appendix</i>	367
<i>References</i>	371
<i>Index</i>	385